

**ÇANKAYA UNIVERSITY**  
**DEPARTMENT OF MATHEMATICS**  
**November.4, 2004**

**Math 257**  
**Mathematics for Electronic Engineers**  
**Midterm 1**

**Duration::90 min.**

**Problems**

1. Find all solutions of the given system of linear equations

$$\begin{aligned}x + y - z + t &= 2 \\2x - y + 2z - t &= -1 \\-x - 4y + 5z - 4t &= 0 \\x - y + 4z - t &= 1\end{aligned}$$

2. Find the rank of the matrix

$$A = \begin{bmatrix} 3 & 1 & 4 \\ 0 & 5 & 8 \\ -3 & 4 & 4 \\ 1 & 2 & 4 \end{bmatrix}.$$

3. Find the value of  $x$  satisfying the equation

$$\begin{vmatrix} 1 & 0 & 3 & 7 \\ 4 & 2 & 0 & 1 \\ 7 & x & 3 & 0 \\ 5 & 0 & x & 8 \end{vmatrix} = 0.$$

4. Is the matrix

$$A = \begin{bmatrix} 0 & -2 & 4 \\ 1 & 0 & -1 \\ 0 & 4 & -7 \end{bmatrix}$$

invertible? If so, find  $A^{-1}$ .

5. Find a basis of eigenvectors and diagonalize. (Show the details)

$$A = \begin{bmatrix} 2 & 0 & 0 \\ -1 & 3 & 1 \\ -1 & 1 & 3 \end{bmatrix}.$$

6. For which values of  $k$  are the following vectors linearly dependent?

$$u = \begin{bmatrix} 2 \\ k \\ -1 \end{bmatrix}, v = \begin{bmatrix} 1 \\ -2 \\ k+1 \end{bmatrix}, w = \begin{bmatrix} 0 \\ 1 \\ 2 \end{bmatrix}.$$